

Find the limit as x approaches a number

$$14A) \lim_{x \rightarrow 2^+} \frac{x}{x+2} =$$

$$14B) \lim_{x \rightarrow 2^-} \frac{x}{x+2} =$$

$$14C) \lim_{x \rightarrow 2} \frac{x}{x+2} =$$

Using the limits found above graph $f(x) = \frac{x}{x+2}$

Vertical Asy.

denominator = 0

Find the vertical asymptotes of the graph and then describe the behavior to the left and right of the vertical asymptote

limit

$$30. f(x) = \frac{1-x}{2x^2 - 5x - 3}$$

$$2x^2 - 5x - 3 = 0$$

$$(2x + 1)(x - 3) = 0$$

$$2x + 1 = 0 \quad x - 3 = 0$$

Horizontal Asy:

$$\lim_{x \rightarrow \pm\infty} f(x) = 0$$

$$\lim_{x \rightarrow -\frac{1}{2}^-} f(x) = \infty$$

$$x = -1 \quad y = \frac{2}{4}$$

$$\lim_{x \rightarrow -\frac{1}{2}^+} f(x) = -\infty$$

$$x = 0 \quad y = \frac{1}{-3}$$

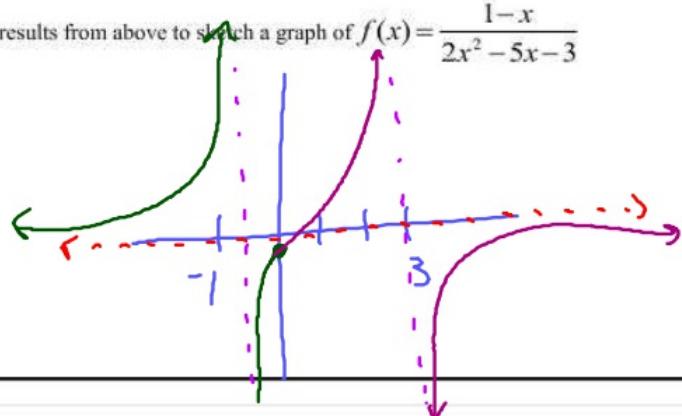
$$\lim_{x \rightarrow 3^-} f(x) = \infty$$

$$x = 2 \quad y = \frac{-1}{-5}$$

$$\lim_{x \rightarrow 3^+} f(x) = -\infty$$

$$x = 4 \quad y = \frac{-3}{9}$$

Use your results from above to sketch a graph of $f(x) = \frac{1-x}{2x^2 - 5x - 3}$



Find the limit of the functions that involve e^x

$$3. \lim_{x \rightarrow \infty} \frac{e^{-x}}{x}$$

$$\lim_{x \rightarrow \infty} \frac{e^{-x}}{x} = -\infty$$

$$\lim_{x \rightarrow \infty} \frac{1}{xe^x} = 0$$

$$A) \lim_{x \rightarrow \infty} \frac{e^x + 2x}{2x} = \infty$$

$$\lim_{x \rightarrow \infty} \left(\frac{e^x}{2x} + \frac{2x}{2x} \right)$$

$$\infty + 1$$

$$B) \lim_{x \rightarrow -\infty} \frac{e^x + 2x}{2x} = 1$$

$$\lim_{x \rightarrow -\infty} \left(\frac{e^x}{2x} + 1 \right)$$

$$(0 + 1)$$

Find the limit of the functions that involve sine and cosine

$$C) \boxed{\lim_{x \rightarrow -\infty} \frac{x^3 + \cos x}{x^3} = 1}$$

$$\lim_{x \rightarrow -\infty} \left(\frac{x^3}{x^3} + \frac{\cos x}{x^3} \right)$$

$$(1 + 0)$$

$$D) \boxed{\lim_{x \rightarrow +\infty} \frac{x^3 + \cos x}{x^3} = 1}$$

$$\lim_{x \rightarrow \infty} \left(\frac{x^3}{x^3} + \frac{\cos x}{x^3} \right)$$

$$(1 + 0)$$

$$E) \lim_{x \rightarrow \infty} \sin\left(\frac{1}{x}\right)$$

$$\lim_{x \rightarrow \infty} \sin\left(\frac{1}{x}\right) \Rightarrow \sin(0) = 0$$

angle approaches 0

$$F) \lim_{x \rightarrow \infty} \frac{\sin\left(\frac{1}{x}\right)}{1 + \left(\frac{1}{x}\right)} = \frac{0}{1 + 0} = 0$$

Find the limit of the functions that involve absolute value

$$8A) \lim_{x \rightarrow \infty} \frac{5x - 2}{|x| - 1} = 5$$

$$8B) \lim_{x \rightarrow -\infty} \frac{5x - 2}{|x| - 1} = -5$$

$$y = \frac{1}{x}$$

